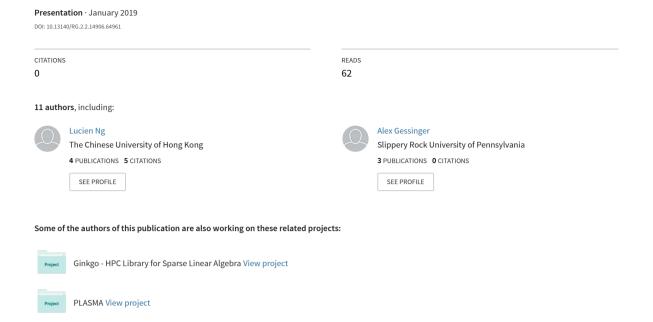
MagmaDNN 0.2 High-Performance Data Analytics for Manycore GPUs and CPUs



MagmaDNN 0.2

High-Performance Data Analytics for Manycore GPUs and CPUs

Lucien Ng¹, Sihan Chen¹, Alex Gessinger⁴, Daniel Nichols³, Sophia Cheng¹, Anu Meenasorna²

¹ The Chinese University of Hong Kong

² National Institute of Technology

³ The University of Tennessee, Knoxville (UTK)

⁴ Slippery Rock University

Kwai Wong^{1,2}, Stanimire Tomov³, Azzam Haidar⁴, Ed D'Azevedo², Jack Dongarra^{3,2}

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² Oak Ridge National Laboratory (ORNL)

³ The Innovative Computing Laboratory, UTK

⁴ Nvidia Corporation

Summer Research Experiences for Undergraduate (REU)
Research Experiences in Computational Science, Engineering, and Mathematics (RECSEM)
Knoxville, TN



Dense Linear Algebra in Applications

Dense Linear Algebra (DLA) is needed in a wide variety of science and engineering applications:

• Linear systems: Solve Ax = b

 Computational electromagnetics, material science, applications using boundary integral equations, airflow past wings, fluid flow around ship and other offshore constructions, and many more

• Least squares: Find x to minimize || Ax – b ||

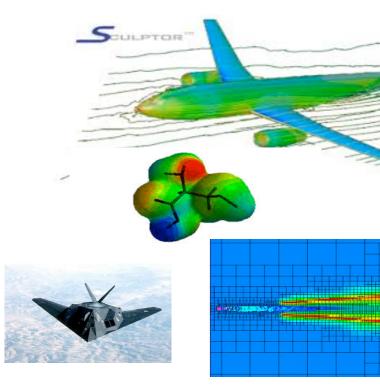
 Computational statistics (e.g., linear least squares or ordinary least squares), econometrics, control theory, signal processing, curve fitting, and many more

• Eigenproblems: Solve $Ax = \lambda x$

 Computational chemistry, quantum mechanics, material science, face recognition, PCA, data-mining, marketing, Google Page Rank, spectral clustering, vibrational analysis, compression, and many more

• SVD:
$$A = U \Sigma V^* (Au = \sigma v \text{ and } A^*v = \sigma u)$$

- Information retrieval, web search, signal processing, big data analytics, low rank matrix approximation, total least squares minimization, pseudo-inverse, and many more
- Many variations depending on structure of A
 - A can be symmetric, positive definite, tridiagonal, Hessenberg, banded, sparse with dense blocks, etc.
- DLA is crucial to the development of sparse solvers



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Provided in MAGMA 2.5

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MAGMA

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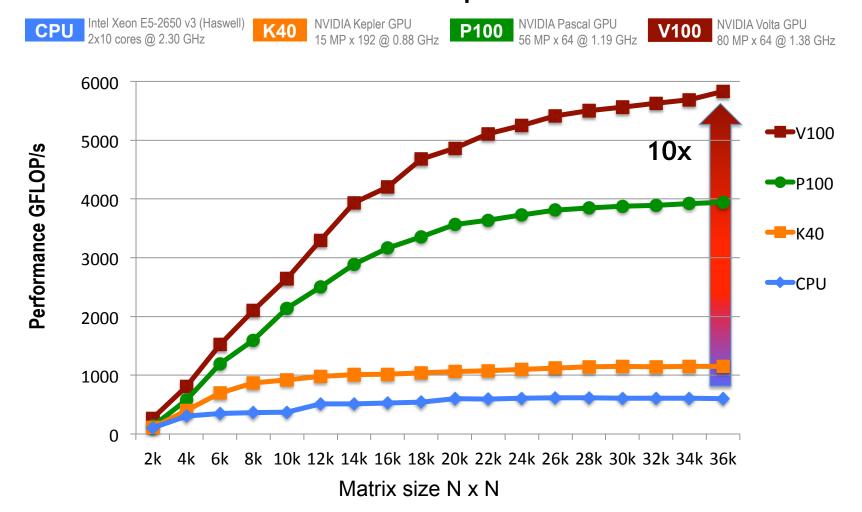
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http://icl.cs.utk.edu/magma https://bitbucket.org/icl/magma Provided in MAGMA 2.5 **FEATURES AND SUPPORT** MAGMA 2.5 FOR CUDA CIMAGMA 1.4 FOR OpenCL MAGMA MIC 1.4 FOR Intel Xeon Phi Linear system solvers Eigenvalue problem solvers **Auxiliary BLAS** Batched LA Sparse LA **CPU/GPU Interface** Multiple precision support Mixed precision (including FP16) Non-GPU-resident factorizations **GPU-only factorizations** Multicore and multi-GPU support MAGMA Analytics/MagmaDNN 0.2 LAPACK testing Linux Windows Mac OS

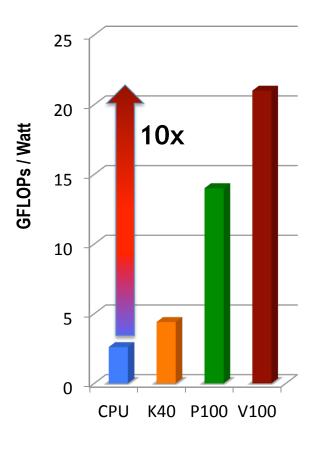
Why use GPUs in HPC?

PERFORMANCE & ENERGY EFFICIENCY

MAGMA 2.5 LU factorization in double precision arithmetic



Energy efficiency (under ~ the same power draw)

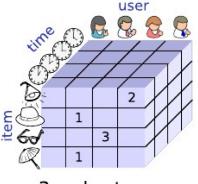


What about accelerated LA for Data Analytics?

- Traditional libraries like MAGMA can be used as backend to accelerate the LA computations in data analytics applications
- Need support for
 - 1) New data layouts, 2) Acceleration for small matrix computations, 3) Data analytics tools

Need data processing and analysis support for Data that is multidimensional / relational

matrix



3 order tensor

Small matrices, tensors, and batched computations



Fixed-size batches



Variable-size batches



Dynamic batches



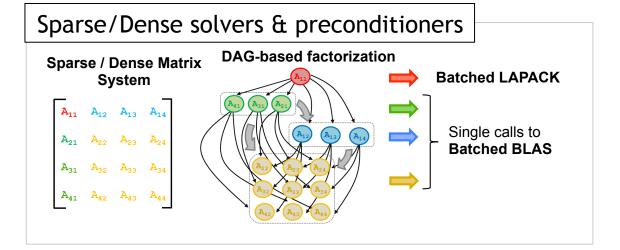
Tensors

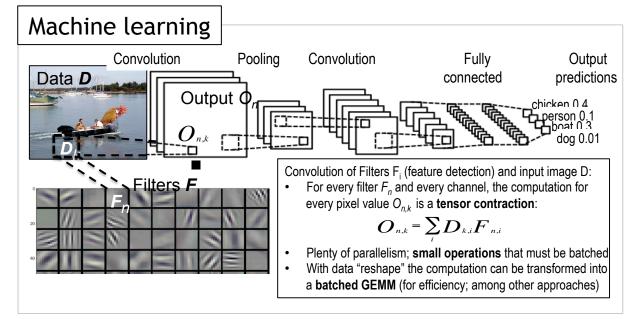
Data Analytics and LA on many small matrices

Data Analytics and associated with it Linear Algebra on small LA problems are needed in many applications:

- Machine learning,
- Data mining,
- High-order FEM,
- Numerical LA,
- Graph analysis,

- Neuroscience,
- Astrophysics,
- Quantum chemistry,
- · Multi-physics problems,
- Signal processing, etc.





Applications using high-order FEM

Matrix-free basis evaluation needs efficient tensor contractions,

$$C_{i1,i2,i3} = \sum_{k} A_{k,i1} B_{k,i2,i3}$$

 Within ECP CEED Project, designed MAGMA batched methods to split the computation in many small high-intensity GEMMs, grouped together (batched) for efficient execution:

Batch_{
$$C_{i3} = A^T B_{i3}$$
, for range of i3 }

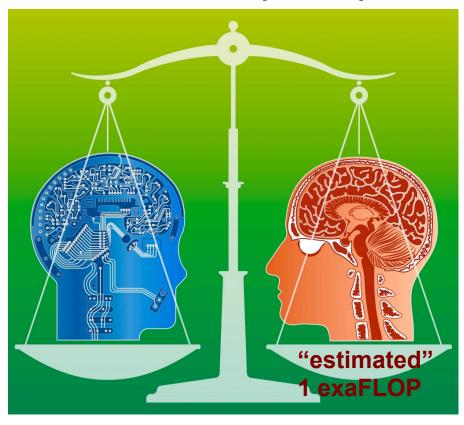
Machine learning / Artificial Intelligence

- Give computers the ability to "learn"
- Soon we may not have to program computers
 - We will train them instead!



See part of GTC'18 Keynote from NVIDIA CEO Jensen Huang https://www.youtube.com/watch?v=oa_wkSmWUw

Human brain vs. supercomputer?

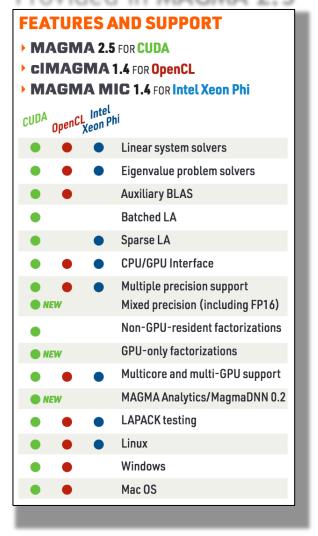


https://www.scienceabc.com/humans/the-human-brain-vs-supercomputers-which-one-wins.html

MagmaDNN - Data Analytics Tool

- MagmaDNN 0.2 HP Data analytics and ML GPU-accelerated numerical software using MAGMA as computational backend to accelerate its LA computations
- Open source; looking for feedback and contributions Started with students from REU/RECSEM program https://bitbucket.org/icl/magmadnn

Provided in MAGMA 2.5



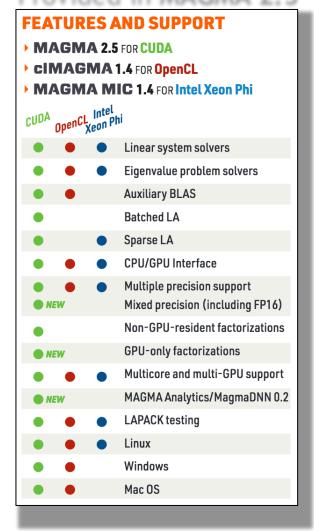
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➤ MagmaDNN 0.2 main functionalities

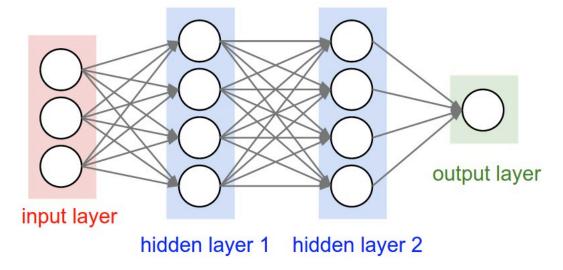
- > Tensors and tensor operations
- Deep learning primitives: Fully-connected layers, convolutional layers, pooling layers, activation layers, and output layers.
- SGD back-propagation training
- Established adapters for calling CuDNN
- Winograd convolutions to accelerate CNNs
- Mixed-precision (FP16-FP32) FFT
- Hyperparameter optimization framework
- ➤ MNIST and CIFAR-10 benchmarks using MagmaDNN
- ➤ Performance comparisons, accuracy validations, etc. (w\ TensorFlow, Theano, and PyTorch)

Provided in MAGMA 2.5



Fully connected layers with MagmaDNN

Fully-connected 3-layer Neural Network example



Data (input, output, NN weights, etc.) is handled through tensor abstractions

// 2d tensor for n_images and n_features in the corresponding dimensions
Tensor<float> Images = Tensor<float>({n_images, n_features});

Support for various layers:

Fully connected (FCLayer), convolution, activation, flatten, pooling, input, output, etc. layers

```
// Create layers for the network

FCLayer<float> *FC1 = new FCLayer<float>(&inputLayer, 128);

ActivationLayer<float> *actv1 = new ActivationLayer<float>(FC1, SIGMOID);

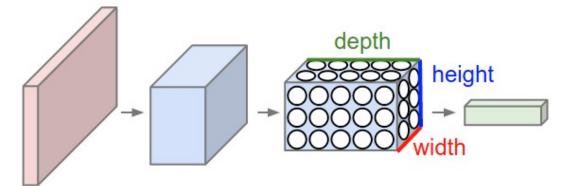
FCLayer<float> *FC2 = new FCLayer<float>(actv1, n_output_classes);
```

> Support networks - composed of layers

```
std::vector<Layer<float>*> vec_layer;
vec_layer.push_back(&inputLayer);
vec_layer.push_back(FC1);
vec_layer.push_back(actv1);
vec_layer.push_back(FC2);
```

Convolutional network layers

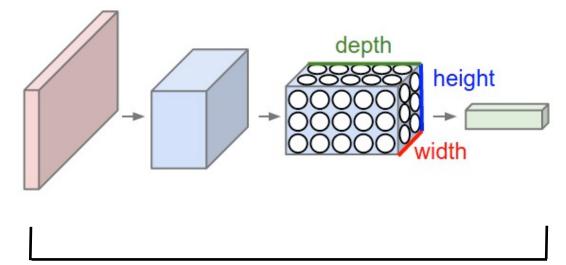
Convolution Network (ConvNet) example



- Layers are typically 3D volumes
- > Handled through tensors
- > Each layer transforms 3D tensor to 3D tensor
- Layers support the forward and backward pass algorithms for the training
- Support for optimization solvers (GD and derivatives)
 - Gradient Descent (GD)
 - Stochastic Gradient Descent (SGD)
 - Mini-Batch Gradient Descent (MB-GD)

How to accelerate on manycore GPU and CPUs?

Convolution Network (ConvNet) example



Require matrix-matrix products of various sizes, including batched GEMMs

- > Convolutions can be accelerated in various ways:
 - Unfold and GEMM
 - > FFT
 - Winograd minimal filtering – reduction to batched GEMMs

Fast Convolution							
Layer	\overline{m}	n	k	M			
1	12544	64	3	1			
2	12544	64	64	1			
3	12544	128	64	4			
4	12544	128	128	4			
5	6272	256	128	8			
6	6272	256	256	8			
7	6272	256	256	8			
8	3136	512	256	16			
9	3136	512	512	16			
10	3136	512	512	16			
11	784	512	512	16			
12	784	512	512	16			
13	784	512	512	16			

Use autotuning to handle complexity of tuning

Accelerating CNNs in MagmaDNN with FFT

 \triangleright Convolutions $D_{i,c} * G_{k,c}$ of images $D_{i,c}$ and filers $G_{k,c}$ can be accelerated through FFT, as shown by the following equality, consequence of the convolution theorem:

$$D_{i,c} * G_{k,c} = FFT^{-1} [FFT(D_{i,c}) * FFT(G_{k,c})],$$

where .* is the Hadamard (component-wise) product, following the '.*' Matlab notation

- > Developed mixed-precision (FP16-FP32) FFT using the GPU's Tensor Cores (TC) acceleration
 - Dynamic splitting to increase the FP16 accuracy, while using high-performance TC

$$X_{FP32}(:) = s_1 X1_{FP16}(:) + s_2 X2_{FP16}(:)$$

[X1 X2] = FFT([X1 X2] in FP16+ (e.g., go to radix 4, where the FFT matrix is exact in FP16)

FFT (X)
$$\approx$$
 s_1 **X1 +** s_2 **X2**

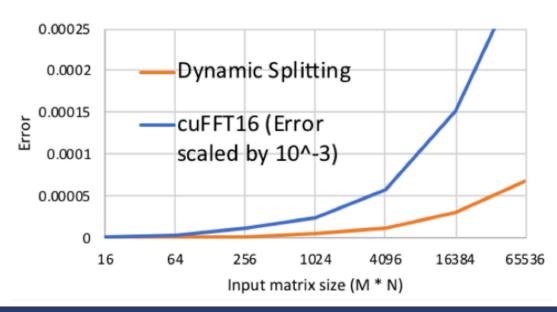
Accelerating CNNs with FFT

Accuracy of the mixed-precision (FP16-FP32) FFT

Reference:

X. Cheng, A. Sorna, Ed D'Azevedo, K. Wong, S. Tomov, "Accelerating 2D FFT: Exploit GPU Tensor Cores through Mixed-Precision," The International Conference for High Performance Computing, Networking, Storage, and Analysis (SC'18), ACM Student Research Poster, Dallas, TX, November 11-16, 2018.

https://icl.utk.edu/projectsfiles/magma/pubs/77-mixed-precision-FFT.pdf https://www.jics.utk.edu/recsem-reu/recsem18



Accelerating 2D FFT: Exploit GPU Tensor Cores through Mixed-Precision

Xiaohe Cheng, Anumeena Sorna, Eduardo D'Azevedo (Advisor), Kwai Wong (Advisor), Stanimire Tomov (Advisor) Hong Kong University of Science and Technology, National Institute of Technology, Oak Ridge National Laboratory, University of Tennessee

Overview

- ☐ 2D FFT in HPC applications
 - Frequency domain analysis
- Quantum cluster simulations
 I arge volume and high parallelism
- Exploit modern parallel architectures
- Graphics Processing Units (GPUs)
- Nyidia CLIDA

 cuFFT library: current state of the art, but can NOT benefit from the FP16 arithmetic on recent hardware due to accuracy limitations

Operation Acceleration

GEMM 320%
FFT FP16 17.02%

cuFFT does not achieve the same level of acceleration as cuBLAS GEMM

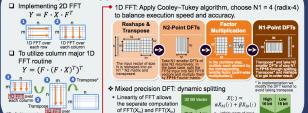
- Results: Tensor Core accelerated FFT & improved accuracy
- Straightforward CUDA implementation costs ~2.5x time of cuFFT32
- Error within 10-4, 1000x better than cuFFT16

Motivation

- ☐ <u>Mixed-precision methods</u> benefit both computation and memory
- Tensor cores on new GPU architecture
 Matrix-multiply-and-accumulate units with throughput up to 125 TFLOPS
- Multiply Inputs: FP16 (half type) only
- ☐ FFT properties: linearity, numerical stability, intensive matrix multiplications
 Our novel implementation that exploits tensor cores by dynamically splitting a

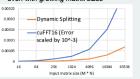
FP32 input into two FP16 operands

Our Proposed Approach



Experimental Results

☐ The method preserves high accuracy, even with growing matrix sizes



The relative error of 2D FFT at different input sizes (horizontal dimension * vertical dimension), using ou implementation and half precision cuFFT.

☐ The implementation can handle a wide range of inputs and produce

T, starrange ±10-7 ±10-2 ±1.0 ±102 ±104 ±109 ufFF16 59.085 5.888 5.6027 5.783 N/A N/A

is not significant

■ GEMM

■ Splitting

☐ The cost of dynamic splitting and combine

About 90% of total time is spent on matrix multiplication

Additional Observations

For fixed number of input elements, the accuracy is affected by the shape of matrix. Particular matrix dimensions lead to higher accuracy, which can be exploited by FFT apolications.

Conclusions & Future Work

- Our dynamic splitting method computes 2D fas transform efficiently by utilizing the hardware advancement in half-precision floating-point ari
- ☐ The implementation effectively emulates single precision calculation, and produces highly according results from a variety of inputs
- The speed of current cuBLAS-based implemen inferior to cuFFT library, but optimizations are a
- Tiled matrix transpose via GPU shared
 Pre-computation of twiddle factors
- Pre-computation of twiddle factors
 Combination of real and imaginary operation
- Combination of real and imaginary operation
 Input-aware auto-tuning splitting algorithm is to designed to support ill-conditioned inputs. It may be a vegetable and appearance are also appearance.

Acknowledgements & Reference

This reject was gozonous by the National Science Foundation through Research Undergonistics (SELI) period with a selfational topout from the Selin butther of Co at University of Tennessee Knowlike. This project used allocations from the Earne Engineering Discovery Environment (SECIE), which is supported by the National addition, the computing work was also performed on technical workstations downline. Performance Computing Team This research is generated by the Office of Advanc Computing Research; U.S. Department of Energy. The work was performed at the Laboratory, which is managed by 17-Selandies, LLC under Cortinat No. De ACOS-O (1) Kumar. Vigin. et al. Introduction to perallel computing design and analysis of all Robeodock Gryb Deginario/Cummings, 1969.

[18] Oddsdein, Deminik, Robert Strzodka, and Stefan Turek, "Performance and accurate, emulations of Judice Portions and Proposition Committee.

Accelerating CNNs with Winograd's minimal filtering algorithm

FFT Convolution is fast for large filters;
Typical filters are small, e.g., 3x3, where Winograds's algorithm has been successful;
In 2D, convolution of tile D of size 4x4 with filter F of size 3x3 is computed as

$$D * F = A^{T} [[G D G^{T}] .* [B^{T} D B]] A$$

where B, G, and A are given on the right:

$$B^{T} = \begin{bmatrix} 1 & 0 & -1 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & -1 & 1 & 0 \\ 0 & 1 & 0 & -1 \end{bmatrix}$$

$$G = \begin{bmatrix} 1 & 0 & 0 \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & -\frac{1}{2} & \frac{1}{2} \\ 0 & 0 & 1 \end{bmatrix}$$

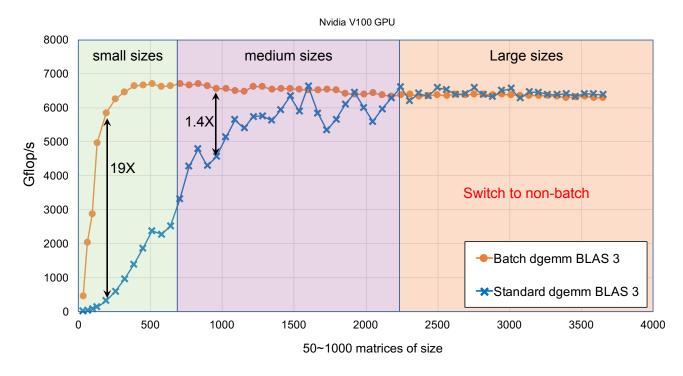
$$A^{T} = \begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & 1 & -1 & -1 \end{bmatrix}$$

➤ Computing for a number of filters, sliding the tile over a batch of images, each with a number of channels, can be expressed as batched gemms, e.g.,

•				
batch	m	n	k	(sizes coming from VGG-16 CONVOLUTION LAYERS)
16x64	12544	64	3	
16x64	12544	64	64	
16x16	12544	128	64	
16 y 16	12544	128	128	

How to implement fast batched DLA?

Problem sizes influence algorithms & optimization techniques



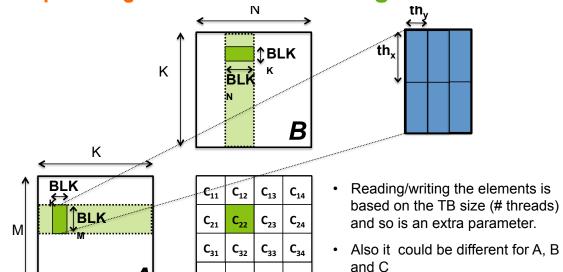
Matrix sizes (fixed) in the batch

Batch size 1.000 Batch size 300

Batch size 50

Kernels are designed various scenarios and parameterized for autotuning framework to find "best" performing kernels

Optimizing GEMM's: Kernel design



Hyperparameter optimization framework

> Hyperparameters are grouped in Model class

```
// put in layers a sequence of predefined layers
std::vector<Layer<float>*> layers { &input_layer, FC1, actv1, FC2, output_layer };
// set some hyperparameters
Param p { learning_rate, weight_decay, batch_size, epochs };
Model model (p, &layers);

// train network model – arguments train data, train outcomes, verbose, accuracy, loss model.fit(x_train, y_trian, false, accuracy, loss);
```

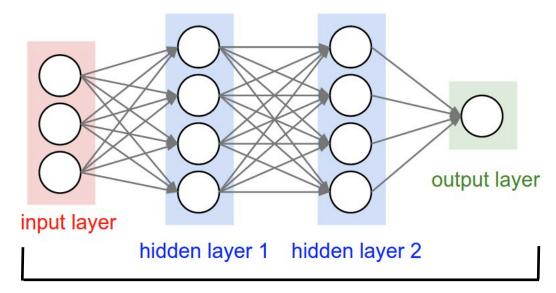
> User can define a hyperparameter search space, e.g., start parameters, end, and step

```
Param start { 0.2, 0, n_batch, 5 };
Param end { 0.2, 1, n_batch, 5 };
Param step { 0.01, 0.01, 1, 1 };
Model model (start, &layers);
```

... and find optimal parameters via a grid_search function
 Param opt = grid_search(model, x_train, y_train, start, end, step, 5, -1, 5000, true);

MagmaDNN benchmarks and testing examples

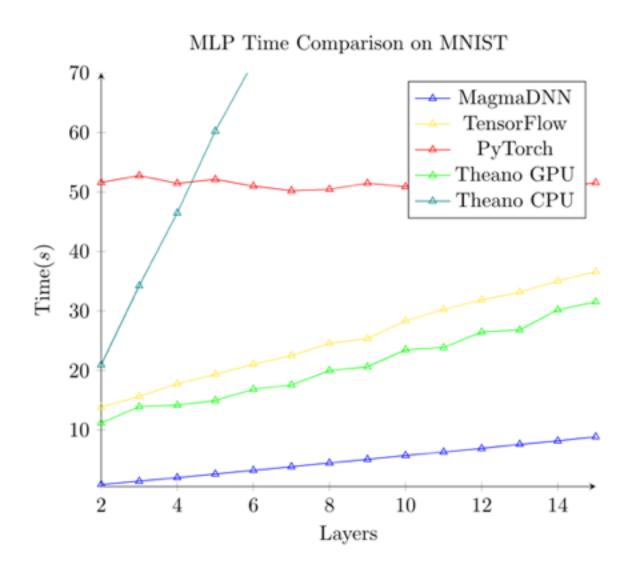
Fully-connected 3-layer Neural Network example



- ➤ The MNIST benchmark is a NN for recognizing handwritten numbers
- ➤ Input for the training are images of handwritten numbers and the labels indicating what are the numbers

- > MagmaDNN has testing/example drivers
- ➤ Example implementing the MNIST benchmark using MagmaDNN multilayer perceptron or a convolutional neural network
- CIFAR-10 benchmark using MagmaDNN
- Benchmarks for Wingrad and FFT
- ➤ Performance comparisons, accuracy validations, etc. (w\ TensorFlow, Theano, and PyTorch)

MagmaDNN performance benchmarks and validations



- MagmaDNN outperforms other popular deep learning libraries
- Compute time scales better than other libraries as models get larger

Parameter/Setting	Value		
Name			
GPU	Nvidia 1050 Ti		
CPU	Intel Xeon X5650 @		
	2.67GHz x 12		
OS	Ubuntu 16.04 LTS		
Epochs	5		
Batch Size	100		
Learning Rate	0.2		
Weight Decay	0.001		
#Hidden Units Layer	528		

MagmaDNN benchmarks and testing examples ...





EEG-Based Control of a Computer Cursor Movement with Machine Learning. Part B

Students: Justin Kilmarx (University of Tennessee), David Saffo (Loyola University), Lucien Ng (The Chinese University of Hong Kong)

Mentors: Xiaopeng Zhao (UTK), Stanimire Tomov (UTK), Kwai Wong (UTK)

Brain-Computer Interface (BCI great interest in the recent year will lead to many possibilities in entertainment fields.

Instead of using invasive BCI, v intention by classifying their El which recorded electrical activ art machine learning technolog advanced prosthetic devices ca patients can be benefited from



Figure 1: A picture cap

To classify the user indent signal with high accuracy. To accelerate the process

Intro A OAK National Laboratory

which is a 2688 by 26

input image I, we tr

three basic modes. It closely represented a

basic modes, namely



Unmixing 4-D Ptychographic Image:

Part B:Data Approach

Student: Zhen Zhang(CUHK), Huanlin Zhou(CUHK), Michaela D. Shoffner(UTK) Mentors: R. Archibald(ORNL), S. Tomov(UTK), A. Haidar(UTK), K. Wong(UTK)

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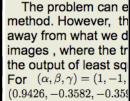
The DFT conve

signals accord



Accelerating FFT with half-precision floating point hardware on GPU

Anumeena Sorna (NITT) & Xiaohe Cheng (HKUST) Mentor: Eduardo D'Azevedo (ORNL) & Kwai Wong (UTK)



A machine learning to achieve better acc an image with (α, β, γ) network is (0.9994, nodes in each hidden 0.01.





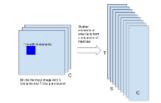
Design and Acceleration of Machine-Learning back-ends on modern Architectures

Students: Alex Gessinger(SRU), Sihan Chen(CUHK) Mentors: Dr. Stanimire Tomov(UTK), Dr. Kwai Wong(UTK)

Abstract

Convolutional Neural Networks are extremely useful in computer vision and many other related fields, but the computation of them tends to be extremely expensive in many cases. The aim of this research project is to accelerate Convolutional Neural Networks, while it is divided into two directions:

- To design a machine-learning back-end on GPU using the MAGMA library to using efficient algorithms;
- To analyze the performance of various machine learning back-ends.



A simple illustration on how to scatter an input image with C channels. We divide it into T tiles (with overlap) of S elements.

The grap implemente of the mode learning rat remained un which consi split 5:1 trai

Current work and Future directions

Performance portability and unified support on GPUs/CPUs

- C++ templates w/ polymorphic approach;
- Parallel programming model based on CUDA, OpenMP task scheduling, and MAGMA APIs.

Hyperparameter optimization

- Critical for performance to provide optimizations that are application-specific;
- A lot of work has been done (on certain BLAS kernels and the approach) but still need a simple framework to handle the entire library;
- Current hyperparameter optimization tool must be further extended in functionalities
- Add visualization and OpenDIEL to support ease of GPU deployment over large scale heterogeneous systems

Extend functionality, kernel designs, and algorithmic variants

- BLAS, Batched BLAS, architecture and energy-aware
- New algorithms and building blocks, architecture and energy-aware
- Randomization algorithms, e.g., for low-rank approximations, and applications

Use and integration with applications of interest (with ORNL collaborators)

- Brain-computer interface systems
- Post-processing data from electron detectors for high-resolution microscopy studies (Unmixing 4-D Ptychographic Images)
- Optimal cancer treatment strategies

Collaborators and Support

MAGMA team

http://icl.cs.utk.edu/magma

PLASMA team

http://icl.cs.utk.edu/plasma







Collaborating partners

University of Tennessee, Knoxville Lawrence Livermore National Laboratory University of California, Berkeley University of Colorado, Denver INRIA, France (StarPU team) KAUST, Saudi Arabia











